

## MATHEMATICAL METHODS – PAPER II

### Unit-I

**Laplace Transforms** – Inverse Laplace Transforms – Error functions – Application to boundary value problems(Heat Equations-Laplace equation) – Fourier transform – Fourier integral formula – Finite & Infinite Fourier sine and cosine transforms – Application to integral equations and Boundary Value problems – Hankel Transform.

### Unit-II

**Special function:** Bessel functions: Recurrence relations for the Bessel co-efficient – Series expansions for Bessel co-efficient – Integral expression for the Bessel co-efficient. The additions formula for the Bessel co-efficient – Legendre's equations – Orthogonal properties of Legendre's polynomials – Hermite polynomials.

### Unit-III

**Numerical solution of partial differential equations** – Introduction – Finite difference approximations to derivatives – Finite difference methods – Laplace's equation – parabolic equations – Cranice – Nicholson Method – Jacobi method – Gauss Siedel method.

### Unit-IV

**Finite Element Methods** – Integral formulation and variational methods : Need for weighted-integral forms – Some mathematical concepts and formulas – Boundary, initial and Eigen value problems – Integral relations – Functionals – The variational symbol – Weak formulation of Boundary value problems – Weighted-Integral and Weak formulations – Linear and Bilinear forms and Quadratic functional – examples. Variational methods of approximation – The Rayleigh – Ritz Method – Petrov-Galerkin method.

### Unit-V

**Variational principles** – Euler's equations – Euler – Lagrange equation- Lagrange Multipliers, Variable end points, Sturm-Liouville problems, integral equations: Introduction, Relations between Differential and Integral Equations, The Green's function, alternative definition of the Green's function, Linear equations in Cause and Effect – The influence function.

### References :

1. **Integral Transforms** – Goyal and Gupta
  2. **Introductory Methods of Numerical Analysis** – S.S.Sastry
  3. **Methods of Applied Mathematics** – Francis B. Hildebrand, PHI Limited
  4. **Special functions of Mathematical physics and Chemistry** – I.N.Sneddon
- Differential Equations** – Elsgoltz

**MATHEMATICAL METHODS – PAPER II**  
**Model question Paper**

**Max. Marks : 100**

**Time : 3 hours**

**Note : 1. Answer any FIVE Questions**

**2. Each Question carries 20 Marks.**

\* \* \*

Q.No.1.

- (a) Find the finite Fourier Sin & Co Sin of  $f(x)=x(\pi-x)$  in  $0 < x < \pi$
- (b) State and Prove the Orthogonality of Bessel Functions
- (c) Using Modified Euler's Method find  $y(0.2)$  and  $y(0.4)$  given

$$\frac{dy}{dx} = y + e^x, \quad y(0) = 0$$

Q.No.2

- a) Evaluate  $L \left[ \frac{1 - \cos t}{t^2} \right]$
- b) Using Convolution Theorem solve  $L^{-1} \left( \frac{s}{(s^2 + a^2)^2} \right)$

Q.No.3

Using Laplace Transform methods solve the D.E.

$$\frac{d^2y}{dt^2} + 2 \frac{dy}{dt} + 5y = e^{-t} \sin t, \quad y(0) = 0, y'(0) = 1$$

Q.No.4

Apply the Fourth order RK-Method to find  $y(0.1)$  and  $y(0.2)$  given  $\frac{dy}{dx} = xy + y^2, y(0) = 1$

Q.No.5

Explain about the Rayleigh-Ritz Method

Q.No.6

- a) If a displacement field is described by  $u = (-x^2 + 2y^2 + 6xy)10^{-4}$   
 $v = (3x + 6y - y^2)10^{-4}$

Determine  $\epsilon_x, \epsilon_y, \gamma_{x,y}$  at the point  $x = 1, y = 0$

b) In a plane strain problem, we have

$$\sigma_x = 20000 \text{ psi}, \sigma_y = -10000 \text{ psi}$$

$$E = 30 \times 10^6 \text{ psi}, \nu = 0.3$$

Determine the value of the stress  $\sigma_z$

Q.No.7

Explain about Cranice – Nicholson Method to solve a partial differential equation.

Q.No.8

Explain about the Sturm-Liouville problem of boundary value problem involving linear ordinary differential equations.